

1. Derive $R = C_p - C_v$ for an ideal gas by considering changes at constant pressure and constant volume (Mayer's equation).
2. Show that for a quasi-static adiabatic process in a perfect gas, with constant specific heats, that

$$pV^\gamma = \text{const.} \quad \text{where} \quad \gamma = \frac{C_p}{C_v}.$$

You will need Mayer's equation.

3. The molar energy of a monatomic gas which obeys van de Waals' equation is given by

$$E = \frac{3}{2}RT - \frac{a}{V}$$

where a is a constant and V is the molar volume at temperature T . From temperature T_1 and volume V_1 the gas is allowed to expand adiabatically into a vacuum so that it occupies a volume V_2 . What is the final temperature of the gas?

4. Two vessels contain the same number N of molecules of the same perfect gas. Initially the two vessels are isolated from each other, the gases being at the same temperature T but at different pressures p_1 and p_2 . The partition separating the two gases is removed. Find the change of entropy of the system when equilibrium has been re-established, in terms of initial pressures p_1 and p_2 . Show that this entropy change is non-negative.
5. By examining variations in E , F , H and G , derive the four different Maxwell relations for the partial derivatives of S , p , T and V .
6. Obtain the partial derivative identity

$$\left. \frac{\partial S}{\partial T} \right|_p = \left. \frac{\partial S}{\partial T} \right|_V + \left. \frac{\partial S}{\partial V} \right|_T \left. \frac{\partial V}{\partial T} \right|_p$$

7. Obtain the partial derivative identity

$$\left. \frac{\partial p}{\partial T} \right|_V \left. \frac{\partial T}{\partial V} \right|_p \left. \frac{\partial V}{\partial p} \right|_T = -1$$