- 1. For each of the 5 Bravais lattices in 2D:
  - (a) Write down the defining properties of a possible pair of lattice vectors (relative lengths and angle between them).
  - (b) Write down the symmetries of the crystal lattice.
  - (c) Find a unit cell and a primitive unit cell, and find the number of lattice sites in each.
- 2. Find an explicit form for the conventional lattice vectors for graphene (see lecture).
- 3. Find the crystal lattice, possible lattice vectors, and a unit cell, for the Kagome lattice (figure 3).

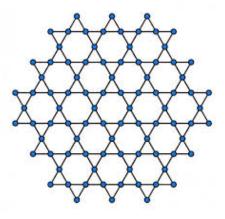


Figure 1: The Kagome lattice.

- 4. Show that  $c/a = \sqrt{8/3}$  for hexagonal close packing of hard spheres.
- 5. Sketch a few cubic unit cells and draw the following lattice planes within them:  $(0\ 0\ 1)$ ,  $(1\ 0\ 1)$ ,  $(0\ 1\ 1)$ ,  $(0\ 2\ 1)$ ,  $(2\ 1\ 0)$ ,  $(2\ 1\ 1)$ , and  $(1\ 2\ 2)$ .
- 6. Prove that in a lattice of cubic symmetry the direction  $[h \, k \, l]$  is perpendicular to the plane  $(h \, k \, l)$  with the same indices.
- 7. Show that the spacing d of the (h k l) set of lattice planes in a cubic lattice of side a is

$$d = \frac{a}{\sqrt{h^2 + k^2 + l^2}}$$

8. Consider the pattern

Indicate:

- (a) a rectangular unit cell;
- (b) a primitive unit cell; and
- (c) the basis of letters associated with each lattice point.
- 9. Consider the fcc, bcc, hcp, and diamond structures.
  - (a) Draw plans of the conventional unit cells of these structures, indicating the height of the atoms as a fraction of the unit cell height.
  - (b) What are the coordinates of the atoms in the basis of each structure.
  - (c) If the structures were formed out of touching spheres, what would be the volume of space they take up as a fraction of the whole?
- 10. A crystal has a basis of one atom per lattice point and a set of primitive translation vectors (measured in Å):

$$a = 3\hat{i}, \qquad b = 3\hat{j}, \qquad c = 1.5\left(\hat{i} + \hat{j} + \hat{k}\right),$$

where  $\hat{i}$ ,  $\hat{j}$ , and  $\hat{k}$  are the standard unit vectors of a Cartesian coordinate system.

- (a) What is the Bravais lattice type of this crystal?
- (b) What are the Miller indices of the set of planes most densely populated with atoms?
- (c) What are the volumes of the primitive unit cell and the conventional unit cell?
- 11. For the fcc and bcc structures it is possible to choose a primitive unit cell where the primitive translation vectors **a**, **b**, and **c** are equal in magnitude, as are the angles between them (a rhomb). Sketch a diagram for each case showing **a**, **b**, and **c** and calculate the angles between them.